

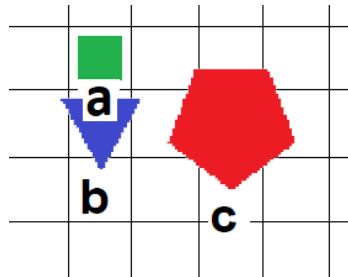
Answers to Problem Set 2

[Total: 50 marks]

1.

- (i) It's invalid, as shown by this TT || F world (where the premises are true and the conclusion is false). [4 marks for world]

- T Adjoins(a, b)
- T SameRow(c, b)
- T LeftOf(a, c)
-
- F SameRow(a, c)

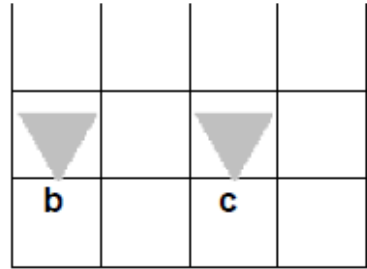


- (ii) Valid. [4 marks for proof outline]

1. Tet(b) \vee Cube(c)
2. Tet(a)
3. \neg SameShape(a, b)
-
4. \neg Tet(b) (2, 3)
5. Cube(c) (1, 4)
6. \neg Dodec(c) (5)

(iii) [4 marks for world]

T	1. SameSize(b, c)
T	2. Tet(c) \wedge Tet(b)
T	3. SameRow(b, c)
<hr/>	
F	4. b = c



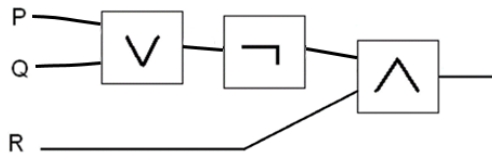
2. Here's a formal proof.
[5 marks for the proof]

1	RightOf(a, c)	
2	a = b	
3	d = c	
4	RightOf(b, c)	= Elim: 1,2
5	d = d	= Intro
6	c = d	= Elim: 3,5
7	RightOf(b, d)	= Elim: 4,6

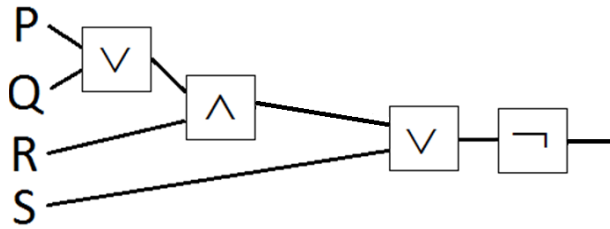
3. [2 marks each]

- (i) $\neg(P \wedge Q)$ Negation sentence
- (ii) $\neg P \vee Q$ Disjunction sentence
- (iii) $(\neg P \wedge Q) \vee R$ Disjunction sentence
- (iv) $(P \wedge Q) \wedge \neg(R \vee S)$ Conjunction sentence

(v) Conjunction sentence



(vi) Negation sentence



4. [1 mark for each truth value -- total 10 marks]

- F 1. $d \neq e$

- T 2. $\text{Dodec}(c) \vee \text{Dodec}(a)$

- T 3. $\text{Cube}(d) \wedge \text{Cube}(e)$

- F 4. $\neg(\text{Cube}(d) \wedge \text{Cube}(f))$

- F 5. $\neg(\text{Cube}(a) \vee \text{Cube}(f))$

- T 6. $\neg(\text{Small}(a) \wedge \neg \text{Small}(f))$

- T 7. $\text{Dodec}(f) \vee \neg \text{Medium}(a) \vee \text{Tet}(e)$

- T 8. $\neg(\text{Large}(c) \wedge \neg \text{Medium}(a)) \vee \neg \neg \text{Small}(f)$

- T 9. $(\text{SameSize}(a, f) \vee \text{SameSize}(d, e) \vee \text{Larger}(c, f)) \wedge \neg \text{Larger}(f, a)$

- T 10. $\neg \neg \neg \neg \text{Medium}(d)$

5. Here's one such world. [5 marks for world]

				▲ a			
	⬠ f						
⬠ c		⬠ d		⬠ e			

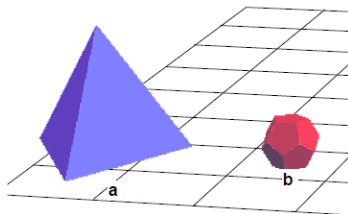
Notes:

- To make #1 true you have to make **d** and **e** non-identical.
- Since **d** remains a cube (by #3) then **f** **cannot be a cube**, to make #4 true. (**f** can be a dodec or a tet.)
- Other worlds are possible, but they require more changes to the original.

6.

(i) [3 marks for world]

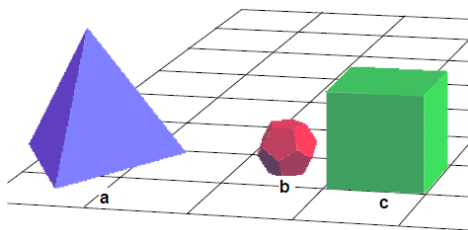
(Note: **b** cannot be large. The size of **a** is irrelevant.)



$$\begin{array}{l|l} T & \neg(\text{Large}(a) \wedge \text{Large}(b)) \\ \hline F & \neg \text{Large}(a) \wedge \text{Large}(b) \end{array}$$

(ii) [3 marks for world]

(Note: **a** must be a tet, and **c** must **not** be a tet. The shape of **b** is irrelevant.)



$$\begin{array}{l|l} T & \text{Tet}(a) \vee (\text{Tet}(b) \wedge \text{Tet}(c)) \\ \hline F & (\text{Tet}(a) \vee \text{Tet}(b)) \wedge \text{Tet}(c) \end{array}$$