THE UNIVERSITY OF BRITISH COLUMBIA

Philosophy 220A

Symbolic Logic I

A THIRD FAKE MIDTERM EXAMINATION

(Originally set on October 25, 2007, UBC)

NAME:			
STUDENT NUMBER:			

SPECIAL INSTRUCTIONS:

Answer all questions. If you get stuck on a question, go on to the next, and return to it later. Indeed, it is wise to read the whole paper before you start, and begin with the easiest questions. Including this cover page, and the sheet of rules, this examination booklet should consist of eight pages. Check that these are all present before the examination begins.

Your answers to all questions should be written in this booklet, in the spaces provided.

For rough work, you may use the plain backs of the sheets in this booklet. If necessary, I can also supply a separate booklet for rough work.

SECTION 003

INSTRUCTOR: Richard Johns

	Cube(x) Medium(x)	- ' '	Larger(x, y) SameRow(x, y)	* ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' '
	<u>a</u> and <u>c</u> aren	't both cubes,	unless they're both	n larger than both <u>d</u> and <u>e</u> .
i)	Provided <u>c</u> is	n't smaller tha	an <u>b, b</u> is larger tha	an <u>a</u> only if <u>c</u> is larger than <u>a</u> .
ii)	(¬Small(a) ∨	∕ ¬ Cube(<i>a</i>)) →	\rightarrow ((Large(a) \lor Med	ium(a)) ∧ Tet(a))
•				
	¬(Cul ¬Dod Adjoi	$be(c) \rightarrow Doo$ $lec(c) \rightarrow Sm$ $lns(c, d) \rightarrow S$	dec(c)) all(c) Small(c)	FrontOf(d, c) \vee Smaller(d, c) c = d \vee Cube(c) \neg (Cube(c) \wedge Dodec(c)) \neg Dodec(c)
	on?	$be(c) \rightarrow Doo$ $lec(c) \rightarrow Sm$ $ins(c, d) \rightarrow S$	dec(c)) all(c) Small(c)	FrontOf(d, c) \vee Smaller(d, c) c = d \vee Cube(c) \neg (Cube(c) \wedge Dodec(c)) \neg Dodec(c)
		$be(c) \rightarrow Doo$ $dec(c) \rightarrow Sm$ $ins(c, d) \rightarrow S$	dec(c)) all(c) Small(c)	FrontOf(d, c) \vee Smaller(d, c) c = d \vee Cube(c) \neg (Cube(c) \wedge Dodec(c)) \neg Dodec(c)
	on? al con?			FrontOf(d, c) \lor Smaller(d, c) c = d \lor Cube(c) \(\sim (Cube(c) \land Dodec(c)) \) \(\sim Dodec(c) \) ces provided with 'yes' or 'no'. [8]

3.	Use a truth table to determine whether or not the following argument is a tautological (TT)
	consequence. Place an asterisk (*) next to any row that is sufficient to determine the answer.
	(There may be no such row. If there is more than one, then mark them all.)
	[8 marks for table]

$$\frac{\left| \underset{(P \leftrightarrow Q)}{P \leftrightarrow} (Q \land R)}{(P \leftrightarrow Q) \land (P \leftrightarrow R)} \right|$$

Answer:		[6 marks]
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4. Show that the following argument is *not* a logically consequence, by constructing an appropriate world. Assume that the rules of "Tarski's World" apply. [12 marks]

RightOf(a, c)
$$\rightarrow$$
 Smaller(a, c)
Medium(c) \leftrightarrow (Cube(c) \land Tet(b))
Small(c) \rightarrow LeftOf(a, c)
 \neg (Large(c) \lor Large(a))
RightOf(a, c) \rightarrow a \neq b

[Draw your world below.]

- 5. For each of the following arguments, prove that the argument is valid by providing a formal proof (in \mathcal{F}) of the conclusion from the premises.
- (i) Write your proof under the premises provided below. [8 marks]

(ii) Write your proof under the premises provided below. [8 marks]

$$\frac{|A \to (B \land C)}{\neg B \to \neg A} \qquad \qquad \boxed{A \to (B \land C)}$$

(iii) Write your proof under the premises provided below. [8 marks]

$$\begin{array}{c|c} \neg^{(D \vee G)} \\ B \to A \\ (D \vee G) \vee (C \to A) \\ \hline (B \vee C) \to A \end{array} \qquad \begin{array}{c|c} \neg(D \vee G) \\ B \to A \\ \hline (D \vee G) \vee (C \to A) \end{array}$$

(iv) Write your proof under the premises provided below. In this proof you may introduce one sentence of the form $P \lor \neg P$ (where P is any FOL sentence) without proof. Cite it as 'Theorem 6.33'. [10 marks]

$$\begin{array}{|c|c|c|c|c|c|}\hline A \longleftrightarrow B & & A \longleftrightarrow B\\\hline (A \land B) \lor (\neg A \land \neg B) & & B \end{array}$$

Total: _____

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